## CSS 322 - QuIz 3 Answers

First name: $\qquad$ Last name: $\qquad$

ID: $\qquad$ Total Marks: $\qquad$
out of 10
Question 1 [3 marks]
Assume you have designed a 4-bit block cipher that produces the following Ciphertext when used with a key $K$ :

| $\mathbf{P}$ | $\mathbf{C}$ | $\mathbf{P}$ | $\mathbf{C}$ | $\mathbf{P}$ | $\mathbf{C}$ | $\mathbf{P}$ | $\mathbf{C}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0000 | 0101 | 0100 | 0010 | 1000 | 1110 | 1100 | 1000 |
| 0001 | 1001 | 0101 | 0111 | 1001 | 1011 | 1101 | 0100 |
| 0010 | 1101 | 0110 | 0000 | 1010 | 1100 | 1110 | 0011 |
| 0011 | 1111 | 0111 | 1010 | 1011 | 0001 | 1111 | 0110 |

If you use your cipher in the Counter mode of operation (with initial value of 0 ), what is the plaintext for the ciphertext $\mathrm{C}=011001001010$ and key $K$.

## Answer

Counter mode encrypts the counter value, and then XORs the result with the ciphertext block to get the original plaintext.
$\mathrm{E}(0000)=0101$
$\mathrm{E}(0001)=1001$
$\mathrm{E}(0010)=1101$
$\mathrm{P}_{1} \quad=\quad \mathrm{C}_{1} \operatorname{XOR} \mathrm{E}(0000)$
$=0110$ XOR 0101
$=0011$
$\mathrm{P}_{2} \quad=\quad \mathrm{C}_{2} \operatorname{XOR} \mathrm{E}(0001)$
$=0100$ XOR 1001
$=1101$
$\mathrm{P}_{3} \quad=\quad \mathrm{C}_{3}$ XOR E(0010)
$=1010$ XOR 1101
$=0111$

Therefore the plaintext is: 001111010111

Question 2 [3 marks]
The following diagram shows the encryption phase of the Output Feedback Mode of operation for 64-bit block ciphers.


Assume you are using a modified Output Feedback Mode that operates on 4-bit block ciphers and it is used with the encryption algorithm designed in Question 2. The plaintext blocks are 2-bits. What is the ciphertext for the plaintext $\mathrm{P}=01101011$ encrypted using key $K$ ? The Initialisation Vector is 0000 .

| Answer |  |  |
| :---: | :---: | :---: |
| IV | = | 0000 |
| Output of Encrypt | = | 0101 |
| $\mathrm{C}_{1} \quad=\mathrm{P}_{1}$ XOR 01 | = | 00 |
| V | = | 0001 |
| Output of Encrypt | = | 1001 |
| $\mathrm{C}_{2}=\mathrm{P}_{2}$ XOR 10 | $=$ | 00 |
| V | = | 0110 |
| Output of Encrypt | = | 0000 |
| $\mathrm{C}_{3}=\mathrm{P}_{3}$ XOR 00 | $=$ | 10 |
| V | = | 1000 |
| Output of Encrypt | = | 1110 |
| $\mathrm{C}_{4}=\mathrm{P}_{4} \mathrm{XOR} 11$ | $=$ | 00 |

Ciphertext $=00001000$

Question 3 [4 marks]
Assume you designed your own encryption algorithm, $A$, which uses 4 -bit blocks and 2-bit keys. The ciphertext for a selection of plaintext and keys for the algorithm, $A$, are given below.

|  | Key |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Plaintext | $\mathbf{0 0}$ | $\mathbf{0 1}$ | $\mathbf{1 0}$ | $\mathbf{1 1}$ |
| $\mathbf{0 0 0 1}$ | 1101 | 0111 | 1101 | 0110 |
| $\mathbf{0 1 0 1}$ | 0000 | 0110 | 0111 | 1010 |
| $\mathbf{0 1 1 1}$ | 0101 | 1101 | 1111 | 0011 |
| $\mathbf{1 0 0 0}$ | 0111 | 1000 | 1100 | 1101 |

To increase the strength of your algorithm, $A$, against brute-force attack, you apply the algorithm twice using a 4-bit key, $K$. The first two bits of $K$ are used as a key into $A$ to encrypt the plaintext to produce output $X$, and the second two bits of $K$ are used as a key into $A$ to encrypt $X$ to produce the ciphertext. You call this new algorithm Double-A.

An attacker has discovered a pair of (plaintext, ciphertext) for Double-A:
(0101, 1101)
a) Use the meet-in-the-middle attack to determine the most likely key $K$ used to produce this ciphertext.
b) A limitation of the meet-in-the-middle attack is the amount of memory needed. Explain why, and give the approximate amount of memory needed to perform the attack on Double-DES (which uses two 56-bit keys)?

## Answer

a)

Encrypting 0101 with a key $\mathrm{K}_{1}$, will produce one of four possible values:

$$
\begin{aligned}
& \mathrm{K}_{1}=00: \mathrm{X}=0000 \\
& \mathrm{~K}_{1}=01: \mathrm{X}=0110 \\
& \mathrm{~K}_{1}=10: \mathrm{X}=0111 \\
& \mathrm{~K}_{1}=11: \mathrm{X}=1010
\end{aligned}
$$

Decrypting 1101 with a key $\mathrm{K}_{2}$, will produce one of four possible values:

$$
\begin{aligned}
& \mathrm{K}_{2}=00: \mathrm{X}=0001 \\
& \mathrm{~K}_{2}=01: \mathrm{X}=0111 \\
& \mathrm{~K}_{2}=10: \mathrm{X}=0001 \\
& \mathrm{~K}_{2}=11: \mathrm{X}=1000
\end{aligned}
$$

Since $X=0111$ matches in both encryption and decryption then the key is: $K_{1}=10, K_{2}=01$, therefore K = 1001.
b)

With the meet-in-the-middle attack, the plaintext is encrypted with every possible key to produce $2^{k}$ values of $X$, each $n$-bits in length. Each value of $X$ needs to be stored in memory for the next phase (decrypting the ciphertext and comparing against the values of $X$ ). For Double-DES this requires approximately 576,000 Terabytes of memory:
$2^{56}$ values of $X$, where $X$ is 64 bits (or 8 bytes) $=576460752303423488$ bytes (approx $5.8 \times 10^{17}$ )

