Public Key Cryptography

Cryptography

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Contents

Concepts of Public Key Cryptography

Public Key vs Symmetric Key

- Symmetric Key Encryption
  - Same key used for encryption and decryption
  - Key is randomly generated (e.g. by sender)
  - *Problem*: How does receiver securely obtain secret key?
- Public (or asymmetric) key encryption
  - Two different, but mathematically related keys
  - One key (public) for encryption, another key (private) for decryption
  - Since encrypt key is public, key exchange is not a problem
  - Ciphers designed around math problems
  - *Problem*: Performance: much, much slower than symmetric

With symmetric key encryption, assume the sender generates a random key. The receiver of the encrypted data must also know that key in order to decrypt the data. But how does the receiver learn the key? If the sender sends the key *unencrypted* then an attacker can learn the key and it is no longer secret. If the sender encrypts the key, then the same problem arises: how do they get the second key (which is used to encrypt the first key) to the receiver?

Public key encryption can solve this problem, as we will see in the following slides.

Symmetric key encryption has been the main form of cryptography for a long time. It wasn't until the 1960's and 1970's that public key cryptography was designed.

Public and Private Keys

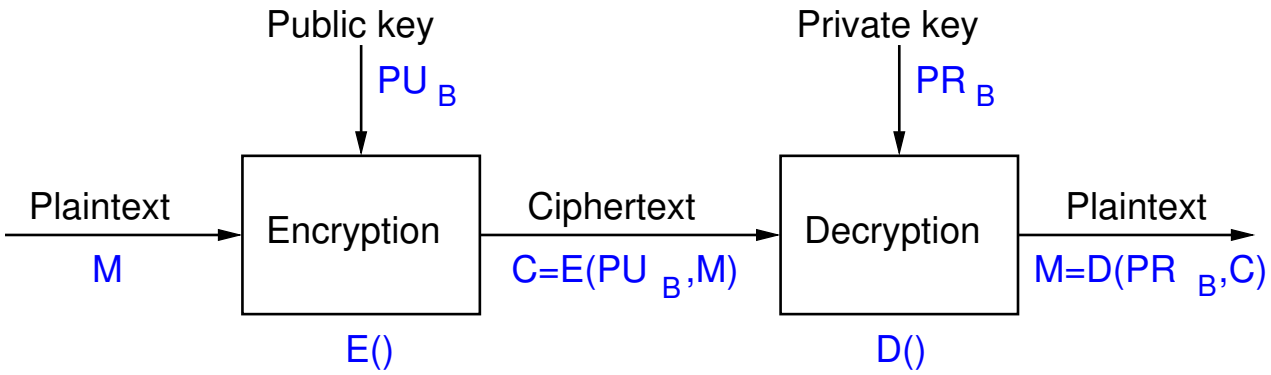
- Every user has their own *key pair*: (PU, PR)
  - Keys are generated using known algorithm (they are not chosen randomly like symmetric keys)
- *Public key*, PU
  - Available to everyone, e.g. in email signature, on website, in newspaper
- *Private key*, PR
  - Secret, known only by owner, e.g. access restricted file on computer
- Ciphers: if encrypt with one key in the pair, can only successfully decrypt with the *other* key in the pair

Consider all the students in the class. With public key crypto, each student would generate their own key pair. They could tell everyone their public key (e.g. yell it out in class, print on the screen and show), but they must keep their private key secret. Note that the keys are related: an algorithm is used to generate them (they are not randomly chosen like symmetric key encryption secret keys). That algorithm must be designed such that it is practically impossible for someone to find the private key if they know the public key.

The encryption/decryption algorithms in public key crypto are designed such that if you encrypt plaintext with one key in the pair, then you can only successfully decrypt the ciphertext if using the other key from that pair. For example, if you encrypt a message with the public key of Steve, then you can only decrypt the ciphertext if you know the private key of Steve.

Some public key ciphers also work in the other direction: if you encrypt a message with the private key of Steve, then you can only decrypt the ciphertext if you know the public key of Steve. We will see this in digital signatures.

Confidentiality with Public Key Crypto



- User A is sender, user B is receiver
- Encrypt using receivers public key, PU_B
- Decrypt using receivers private key, PR_B
- Only B has PR_B, therefore only B can successfully decrypt $\rightarrow$ confidentiality

This assumes User A (on the left) already knows the public key of user B. Since it is PUBLIC there is no problem with A knowing B's public key. However in practice, there are problems with A being sure that the public key does indeed belong to B (maybe it is someone pretending to be B). We don't cover that here, but in the chapter on digital certificates we will see this issue (of knowing who's public key it is) be addressed.

Why Does Public Key Crypto Work?

- Public key ciphers consist of:
  - Key generation algorithm
  - Encryption algorithm
  - Decryption algorithm
- Designed around computationally hard mathematical problems
- Very hard to solve without key, i.e. trapdoor functions
  - Finding prime factors of large integers
  - Solving logarithms in modulo arithmetic
  - Solving logarithms on elliptic curves

The details of the algorithms are covered in subsequent chapters.

Public Key Crypto Examples

- RSA (Rivest Shamir Adleman)
  - Security depends on difficult to factor large integers
  - Widely used for digital signatures
- Diffie-Hellman
  - Security depends on difficult to solve logarithms in modulo arithmetic
  - Widely used for secret key exchange
- Elliptic Curve
  - Security depends on difficulty to solve logarithms on elliptic curve
  - Newer, used in signatures and key exchange
  - Smaller keys is benefit